## MATHEMATICS

## PAPER 1

## Question-Answer Book

## Secondary 2

Date: $\quad$ 19-06-2008
Time: $\quad 8: 30 \mathrm{am}-9: 45 \mathrm{am}$


1. Write your class, class number in the spaces provided on this cover.
2. This paper consists of TWO sections, A and B. Section A and Section B carry 80 marks and 40 marks respectively.
3. Attempts ALL questions in this paper. Write your answer in the spaces provided in this Question-Answer Book.
4. Unless otherwise specified, all working must be clearly shown.
5. Unless otherwise specified, numerical answers should either be exact or correct to 3 significant figures.
6. The diagrams in this paper are not necessarily drawn to scale.

|  | Teacher's Use Only |  |
| :---: | :---: | :---: |
| Section A <br> Question No. | Max. <br> Marks | Marks |
| $\mathbf{1 .}$ | 4 |  |
| $\mathbf{2 .}$ | 6 |  |
| 3. | 6 |  |
| $\mathbf{4 .}$ | 8 |  |
| $\mathbf{5 .}$ | 9 |  |
| $\mathbf{6 .}$ | 10 |  |
| 7. | 10 |  |
| $\mathbf{8 .}$ | 13 |  |
| 9. | 14 |  |
| 10. | 20 |  |
| $\mathbf{1 1 .}$ | 20 |  |
| Total | 120 |  |

## SECTION A Short questions. (80 marks)

1. Without using calculator, find the length of $A B$ in the figure below. (4 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
2. The scale of a map is $1: 200,000$.
a. If a river measures 8 cm long on the map, find the actual length (in km ) of the river. (3 marks)
b. If 2 villages is 30 km apart, what is the distance (in cm ) between the 2 villages on the map. (3 marks)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. A metal cube of side $=5 \mathrm{~cm}$ is melted and recast into a prism with a cross-section in the shape of a sector. If the radius of the sector is 6 cm and the angle at the centre of the sector is $40^{\circ}$, find the height of the prism. (6 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
4. A sum of $\$ 900$ is divided among $A, B$ and $C$ so that $B$ gets twice as much as $A$, and $C$ gets three times as much as B. Find
a. A's share : B's share.
b. A's share : B's share : C's share. (show your workings)
c. amount of A's share.
(3 marks)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
5. Simplify $\frac{90 x^{2}-40}{6 a+6 x-4-9 a x}$
6. In the figure, $\angle \mathrm{EFG}=f$ and 'the reflex angle EFG ' $=4 f$, $\mathrm{EF} / / \mathrm{GJ}, \mathrm{IH} / / \mathrm{FG}$ and $j=108^{\circ}$.
a. Find the unknowns $f, g$ and $h$.
b. Prove that $\mathrm{HI} / / \mathrm{KJ}$.
(7 marks)
(3 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
7. In the diagram below, ABCDEFGH is a regular octagon, EFI and HGIJ are straight lines.
Find the size of each interior
a.
angle of the octagon.
(3 marks)
(7 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
8. In the figure, ABCD is a rectangle with $\mathrm{AD}=12 \mathrm{~cm}$. E is a point on $A B$ such that $A E=9 \mathrm{~cm}$ and $C E=20 \mathrm{~cm}$.
a. Prove that $\triangle \mathrm{CDE}$ is a right-angled triangle.
(11 marks)
b.

Find the area of $\triangle \mathrm{CDE}$.
(2 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
9. Study the diagram given and find the following. A
a. length of AP.
(2 marks)
b. length of AC
(4 marks)
c. Hence, $\angle \mathrm{ABC}$.
(8 marks)

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## SECTION B Long questions (40 marks)

10. Answer this question without using calculator.
a. If $\left(40^{\circ}+\theta\right)+\phi=90^{\circ}$, express $\psi$ in term of $\theta$.
b. Hence or otherwise, prove that $\frac{\cos \left(40^{\circ}+\theta\right)}{\tan \left(50^{\circ}-\theta\right)}=\sin \left(40^{\circ}+\theta\right)$ is an identity. (6 marks)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
11. c. Using $\frac{\cos \left(40^{\circ}+\theta\right)}{\tan \left(50^{\circ}-\theta\right)} \equiv \sin \left(40^{\circ}+\theta\right)$, find the measure of $\theta$ if
i. $\frac{\cos \left(40^{\circ}+\theta\right)}{\tan \left(50^{\circ}-\theta\right)}=\frac{\sqrt{2}}{2}$
ii. $\frac{\cos \left(40^{\circ}+\theta\right)}{\tan \left(50^{\circ}-\theta\right)}=\sqrt{1-\sin ^{2} \theta}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
12. The height and the radius of a solid cylinder are 10 cm and 4 cm respectively. A $\frac{1}{4}$ - cylinder of the same radius and height $=h \mathrm{~cm}$ is cut out from the original cylinder so that the volume of the $\frac{1}{4}$-cylinder is $\frac{3}{17}$ that of the remaining portion as shown in the figure. Find
a. the cross-section area of the cut out portion.
b. the volume of the original cylinder.
(2 marks)
c. $h$, the height of the $\frac{1}{4}$ - cylinder being cut out.
(2 marks)
d. the total surface area of the remaining portion.

(7 marks)
(Give the answers in term of $\pi$.)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
